

Name:

Homework 8, due Wednesday 9/25/2013.

Problem 1: A transmission line has $R'=4.2 \text{ m}\Omega/\text{m}$, $L'=2.1 \text{ }\mu\text{H}/\text{m}$, $C'=5.5 \text{ pF}/\text{m}$, and $G'=0.26 \text{ nS}/\text{m}$. The frequency is 1 kHz. Find (a) the characteristic impedance of the line Z_0 , (b) propagation constant γ , (c) phase velocity u_p , and (d) wavelength λ .

Problem 2: A coaxial cable has its conductors made of copper ($\sigma_c=5.8 \times 10^7 \text{ S}/\text{m}$) and its dielectric made of polyethylene ($\epsilon_r=2.25$, $\mu_r=1$). If the radius of the outer conductor is 3 mm, determine the radius of the inner conductor so that $Z_0=75\Omega$.

Problem 3: On a distortion-less transmission line, the voltage wave is given by:

$$V(x)=120e^{0.0025x}\cos(10^8t+2x)+60e^{-0.0025x}\cos(10^8t-2x)$$

Where x is the distance from the load. If $Z_L=300$, find (a) attenuation constant α , (b) phase constant β , (c) phase velocity u_p , (d) characteristic impedance Z_0 , and (e) the current at x $I(x)$.

Problem 4: A transmission line has a characteristic impedance of $Z_0=65+j38 \text{ }\Omega$, a propagation constant of $\gamma=0.7+j2.5 \text{ m}^{-1}$, and length of $x=0.8 \text{ m}$. Find the input impedance and voltage standing wave ratio of the line if the end of the line is (a) open-circuited, (b) short circuited, (c) impedance matched (d) connected to a load with $Z_L=j27 \text{ }\Omega$.
